GCE

Mathematics B (MEI)

H630/02: Pure Mathematics and Statistics

Advanced Subsidiary GCE

Mark Scheme for June 2019

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This mark scheme is published as an aid to teachers and students, to indicate the requirements of the examination. It shows the basis on which marks were awarded by examiners. It does not indicate the details of the discussions which took place at an examiners' meeting before marking commenced.

All examiners are instructed that alternative correct answers and unexpected approaches in candidates' scripts must be given marks that fairly reflect the relevant knowledge and skills demonstrated.

Mark schemes should be read in conjunction with the published question papers and the report on the examination.

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Annotations and abbreviations

Annotation in scoris	**Meaning**
✓and ✗	
BOD	Benefit of doubt
FT	Follow through
ISW	Ignore subsequent working
M0, M1	Method mark awarded 0, 1
A0, A1	Accuracy mark awarded 0, 1
B0, B1	Independent mark awarded 0, 1
SC	Special case
^	Omission sign
MR	Misread
Highlighting	
Other abbreviations in mark scheme	**Meaning**
E1	Mark for explaining a result or establishing a given result
dep*	Mark dependent on a previous mark, indicated by *
cao	Correct answer only
oe	Or equivalent
rot	Rounded or truncated
soi	Seen or implied
www	Without wrong working
AG	Answer given
awrt	Anything which rounds to
BC	By Calculator
DR	This indicates that the instruction **In this question you must show detailed reasoning** appears in the question.

Subject-specific Marking Instructions for A Level Mathematics B (MEI)

a Annotations should be used whenever appropriate during your marking. The A, M and B annotations must be used on your standardisation scripts for responses that are not awarded either 0 or full marks. It is vital that you annotate standardisation scripts fully to show how the marks have been awarded. For subsequent marking you must make it clear how you have arrived at the mark you have awarded.

b An element of professional judgement is required in the marking of any written paper. Remember that the mark scheme is designed to assist in marking incorrect solutions. Correct solutions leading to correct answers are awarded full marks but work must not be judged on the answer alone, and answers that are given in the question, especially, must be validly obtained; key steps in the working must always be looked at and anything unfamiliar must be investigated thoroughly. Correct but unfamiliar or unexpected methods are often signalled by a correct result following an apparently incorrect method. Such work must be carefully assessed. When a candidate adopts a method which does not correspond to the mark scheme, escalate the question to your Team Leader who will decide on a course of action with the Principal Examiner.
If you are in any doubt whatsoever you should contact your Team Leader.

c The following types of marks are available.

M
A suitable method has been selected and *applied* in a manner which shows that the method is essentially understood. Method marks are not usually lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, e.g. by substituting the relevant quantities into the formula. In some cases the nature of the errors allowed for the award of an M mark may be specified.

A
Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated Method mark is earned (or implied). Therefore M0 A1 cannot ever be awarded.

B
Mark for a correct result or statement independent of Method marks.

E
A given result is to be established or a result has to be explained. This usually requires more working or explanation than the establishment of an unknown result.

Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a correct form of answer is ignored. Sometimes this is reinforced in the mark scheme by the abbreviation isw. However, this would not apply to a case where a candidate passes through the correct answer as part of a wrong argument.

d When a part of a question has two or more 'method' steps, the M marks are in principle independent unless the scheme specifically says otherwise; and similarly where there are several B marks allocated. (The notation 'dep*' is used to indicate that a particular mark is dependent on an earlier, asterisked, mark in the scheme.) Of course, in practice it may happen that when a candidate has once gone wrong in a part of a question, the work from there on is worthless so that no more marks can sensibly be given. On the other hand, when two or more steps are successfully run together by the candidate, the earlier marks are implied and full credit must be given.

e The abbreviation FT implies that the A or B mark indicated is allowed for work correctly following on from previously incorrect results. Otherwise, A and B marks are given for correct work only – differences in notation are of course permitted. A (accuracy) marks are not given for answers obtained from incorrect working. When A or B marks are awarded for work at an intermediate stage of a solution, there may be various alternatives that are equally acceptable. In such cases, what is acceptable will be detailed in the mark scheme. If this is not the case please, escalate the question to your Team Leader who will decide on a course of action with the Principal Examiner.
Sometimes the answer to one part of a question is used in a later part of the same question. In this case, A marks will often be 'follow through'. In such cases you must ensure that you refer back to the answer of the previous part question even if this is not shown within the image zone. You may find it easier to mark follow through questions candidate-by-candidate rather than question-by-question.

f Unless units are specifically requested, there is no penalty for wrong or missing units as long as the answer is numerically correct and expressed either in SI or in the units of the question. (e.g. lengths will be assumed to be in metres unless in a particular question all the lengths are in km, when this would be assumed to be the unspecified unit.) We are usually quite flexible about the accuracy to which the final answer is expressed; over-specification is usually only penalised where the scheme explicitly says so. When a value is given in the paper only accept an answer correct to at least as many significant figures as the given value. This rule should be applied to each case. When a value is not given in the paper accept any answer that agrees with the correct value to 2 s.f. Follow through should be used so that only one mark is lost for each distinct accuracy error, except for errors due to premature approximation which should be penalised only once in the examination. There is no penalty for using a wrong value for *g*. E marks will be lost except when results agree to the accuracy required in the question.

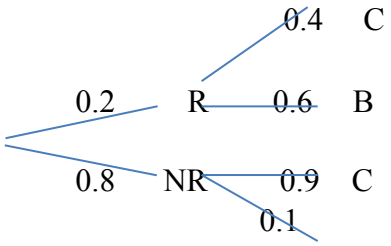
g Rules for replaced work: if a candidate attempts a question more than once, and indicates which attempt he/she wishes to be marked, then examiners should do as the candidate requests; if there are two or more attempts at a question which have not been crossed out, examiners should mark what appears to be the last (complete) attempt and ignore the others. NB Follow these maths-specific instructions rather than those in the assessor handbook.

h For a genuine misreading (of numbers or symbols) which is such that the object and the difficulty of the question remain unaltered, mark according to the scheme but following through from the candidate's data. A penalty is then applied; 1 mark is generally appropriate, though this may differ for some units. This is achieved by withholding one A mark in the question. Marks designated as cao may be awarded as long as there are no other errors. E marks are lost unless, by chance, the given results are established by equivalent working. 'Fresh starts' will not affect an earlier decision about a misread. Note that a miscopy of the candidate's own working is not a misread but an accuracy error.

i If a graphical calculator is used, some answers may be obtained with little or no working visible. Allow full marks for correct answers (provided, of course, that there is nothing in the wording of the question specifying that analytical methods are required). Where an answer is wrong but there is some evidence of method, allow appropriate method marks. Wrong answers with no supporting method score zero. If in doubt, consult your Team Leader.

j If in any case the scheme operates with considerable unfairness consult your Team Leader.

Question			Answer	Marks	AOs		Guidance
1			$4 = 7x^{\frac{1}{2}}$ or $\frac{x^{\frac{1}{2}}}{4} = \frac{1}{7}$	M1	1.1a	Order of M marks may vary. For getting their x term in numerator	$\frac{4}{x^{\frac{1}{2}}} = 7$ not suff for this mark
			Square both sides	M1	1.1a	eg $\frac{x}{16} = \frac{1}{49}$	
			$x = \frac{16}{49}$	A1	1.1		
				[3]			
2			½ × 14 × 8 sin117°	M1	1.2	Condone omission of ½	
			49.9 [cm^2]	A1		Accept 50	50.0 is wrong
				[2]			
3			LHS is (√9×√2) = √18	B1	2.1	OR LHS squared is 18	No calculator. No decimal values allowed.
			RHS is (√4×√3) = √12	B1	1.1	RHS squared is 12	
			√18 > √12 oe (so 3√2 > 2√3)	E1	2.4	AG OR eg √3 × √3 × √2 > √2 × √2 × √3 $\sqrt{3} > \sqrt{2}$, which is true	Allow proof that starts with answer, and shows it must be true.
				[3]			
4	(a)		$(x \pm 4)^2$ and $(y \pm 3)^2$ seen	M1	3.1a	$(x + 4)^2 - 4^2 + (y - 3)^2 - (-3)^2 - 39 = 0$	
			centre is (– 4, 3)	A1	1.1	www	
				[2]			

Question			Answer	Marks	AOs		Guidance
	(b)		radius is 8	B1 [1]	1.1		
5	(a)		 C: cycles B: catches bus R: raining NR :not raining	M1 A1 A1 [3]	1.1 1.1 1.1	correct structure outcomes correct probabilities correct Key not required accept NC: does not cycle	Accept variations on labelling if meaning clear
5	(b)		0.2×0.4 or 0.8×0.9 $0.2 \times 0.4 + 0.8 \times 0.9$ 0.8 cao	M1 A1 A1 [3]	3.1b 1.1 1.1	Ft (a) Ft (a) Accept $\frac{4}{5}$ or 80%	Accept fractions Working may be on diagram in (a)
5	(c)		(their 0.8)^5 0.328 or 0.3277 or 0.32768	M1 A1 [2]	2.1 1.1	$\frac{1024}{3125}$; accept 0.33; accept as percentage	

6	**(a)**		Correct structure for two boxplots seen Range correct and clear on one diagram IQR correct and clear on one diagram Median correct and clear on one diagram Both boxplots completely correct with all details shown as above	**B1** **B1** **B1** **B1** **B1** **[5]**	**1.1a** **1.1** **1.1** **1.1** **1.1**	 F: 82.1 to 86.7 M: 77.6 to 83.3 F: 83.45 to 84.9 M 79 to 81.15 F: 84 M: 80.25 F /M label or with key	Through template circles
6	**(b)**		80.25 < 84 so typical male has lower life expectancy than typical female 2.15 > 1.45 OR 5.7 > 4.6 so life expectancy of males is more variable	**E1** **E1** **[2]**	**2.2a** **2.2a**	OR 80.2844 < 84.2313 so the average life expectancy is lower for males OR 1.4294 > 1.1563 so life expectancy of males is more variable	Or median (or mean) life expectancy for males is less than for females Or life expectancy for males is more variable than for females + ref to range, IQR or sd
6	**(c)**		eg The LDS deals with averages, not individuals, so it does not mean that everyone in London has a longer life expectancy than everyone in Lancashire eg There is no info available for Lancashire	**E1** **E1** **[2]**	**2.4** **2.4**	Any two valid different comments	
6	**(d)**		Either M: 80.2844 ± 2×1.4294 (= 83.1432) or F: 84.2313 ± 2×1.1563 = (86.5439) 83.1(432) < 83.3 and 86.5(439) < 86.7	**M1** **A1** **[2]**	**1.1** **2.4**	Correct use of criterion Both correct comparisons	83.1(432) or 81.9(187) or 86.5(439) or 77.4(256)

6	**(e)**		(linear) **correlation** (strong) **positive**	**M1** **A1** **[2]**	**2.2b** **1.1**		
7	**(a)**		$\int(15x^4+11x^{\frac{8}{3}})\,dx.$ $\frac{15x^5}{5}+\frac{11x^{\frac{11}{3}}}{\frac{11}{3}}[+c]$ $3x^5+3x^{\frac{11}{3}}+c$ oe	**M1** **A1** **M1** **A1** **A1** **[5]**	**3.1a** **1.1** **1.1** **1.1** **3.2a**	Expands bracket with one term correct All correct integration with one term correct FT both terms correct coefficients must be simplified and must see + *c* either here or in previous step	
7	**(b)**		F[8] – F[0] = $3\times8^5 + 3\times2^{11}$ [– 0] eg $(3\times2^4 + 3)\times2^{11}$ 51×2^{11}	**M1*** ***M1** **A1** **[3]**	**2.1** **2.4** **1.1**	or $3\times2^{15} + 3\times2^{11}$ [– 0] ft (a) any correct intermediate step	OR $104448 \div 2^{11}$ (M2)
8	**(a)**		$[\frac{19.8}{36}$ =] 0.55	**B1** **[1]**	**1.1**	or $\frac{11}{20}$	Must be dec or simplified frac; but condone 55%
8	**(b)**		0.0380(96943116…) BC	**B1** **[1]**	**1.1**	Correct to at least 2 sf	Allow truncated

8	**(c)**		H_0: $p = 0.45$ H_1: $p < 0.45$	**B1**	**1.1**	OR H_0: $p = 0.55$ H_1: $p > 0.55$	Both hypotheses
			p is the probability that a driver speeding / caught speeding / on speed awareness course is female	**B1$**	**2.5**	p is the probability that a driver speeding / caught speeding / on speed awareness course is male	Must not be inconsistent with H_1
			Use or sight of B(25, 0.45)	**M1***	**3.3**	OR Use or sight of B(25, 0.55)	Can be implied by P($X = 7$) (OR P($X = 18$)) = 0.038..
			P($X \leq 7$) = 0.06385(0773831)	**A1**	**1.1**	P($X \geq 18$) = 1 – P($X \leq 17$) = 1 – 0.936149 = 0.06385	
			0.06385 > 0.05	***M1**	**3.4**	FT their probability	
			Result is NOT significant or "accept H_0"	**B1**	**1.1**	Dep on 0.06385	May be incorporated in conclusion
			There is insufficient evidence (at the 5% level) to suggest that drivers speeding / caught speeding / on speed awareness course are more likely to be male. oe	**E1**	**2.2b**	Dep all previous marks except B1$	Not assertive
				[7]		SC: Use of p = 0.5 can score B1B1M1 (can be implied by 0.0216 or 0.0143) A0M1B0E0	
8	**(d)**		eg Each driver speeding / caught speeding has the same (constant) probability of being selected for the speed awareness course.	**E1**	**2.4**	OR the probability of any particular driver caught speeding being selected for the speed awareness course is independent of any other driver caught speeding being selected.	
				[1]			

9	(a)		$m = \frac{3.58-3.93}{4-0}$ $\log_{10}V = -0.0875t + 3.93$	M1 M1 A1 [3]	1.1 3.3 1.1	(±) 0.0875 oe Allow any value for – 0.0875 condone omission of base	Condone ln
9	(b)		$V = 10^{-0.0875t + 3.93}$ $A = 10^{3.93} = 8500$ $b = 10^{-0.0875} = 0.82$	M1 A1 A1 [3]	3.1b 3.3 1.1	Or $\log V = \log A + \log b^t$ Accept $V = 8500\times0.82^t$	8511.38 0.81752; sc B1 if both answers not to 2 sf. Allow 8500 taken from table (M1A1)
9	(c)		3151.29 (≈ 3150) so the model is a (very) good fit	E1 [1]	3.4	Must see value from model OR find value of t (approx. 4.98) when model gives 3150	Eg 3107.93 from more accurate values.
9	(d)		$8500\times0.82^t = 500$ soi take logs of both sides (t = 14.27 so) after 15 years	M1 M1 A1 [3]	3.1b 1.1 3.5a	Ft from (b) for M1M1 eg $\log8500 + \log0.82^t = \log500$; can be implied by 15 or 14.(…)	or $\log0.82^t = \log(\frac{500}{8500})$

10			$x = 2, y = 3$	**B1**	**1.1**		soi
			$\frac{dy}{dx} = \frac{2x}{4} - \frac{2}{x^2}$ oe	**M1**	**2.1**	Differentiation with 1 term correct	
				A1	**1.1**		
			Evaluaton of their derivative at $x = 2$	**M1**	**1.1**	NB ½	
			$y - 3 = ½(x - 2)$	**M1**	**2.4**	equation of tangent	$y = \frac{1}{2}x + 2$
			$y - 3 = -2(x - 2)$	**M1**	**1.1**	and equation of normal; FT their tangent gradient	$y = -2x + 7$
			intercepts are $(-4, 0)$	**A1**	**1.1**		
			and $(3.5, 0)$	**A1**	**1.1**		
			Area $= \frac{1}{2} \times 7\frac{1}{2} \times 3$	**M1**	**2.1**	OR $\frac{1}{2} \times \sqrt{(6^2 + 3^2)} \times \sqrt{(3^2 + 1.5^2)}$ - lengths of tangent and normal	May see $3\sqrt{5}$ and $\frac{3}{2}\sqrt{5}$ – or integration (complete method)
			$\frac{45}{4}$ cao	**A1**	**1.1**	or 11.25	
				[10]			

OCR (Oxford Cambridge and RSA Examinations)
The Triangle Building
Shaftesbury Road
Cambridge
CB2 8EA

OCR Customer Contact Centre

Education and Learning
Telephone: 01223 553998
Facsimile: 01223 552627
Email: general.qualifications@ocr.org.uk

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Facsimile: 01223 552553

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